

Learning Intentions

- Learn how rolling resistance relates to the force of friction.
- Learn how to calculate the force of friction and the coefficient of friction.

Definitions and Formulas

1. Force of gravity:

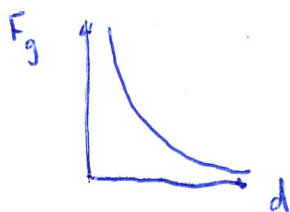
$$\vec{F}_g = m\vec{g}$$

Force of gravity (Newtons) ← \vec{F}_g

mass (kg) ← m

Acceleration due to gravity
On Earth, $\vec{g} = 9.81 \text{ m/s}^2 = 9.81 \text{ N/kg}$ [down] ← \vec{g}

2. Universal Law of Gravitation:



$$F_g = \frac{Gm_1m_2}{d^2}$$

G = gravitational constant = $6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg}\cdot\text{s}^2}$
 m = mass of object (kg)
 d = distance between centres of objects (m)

- a. The law is not actually universal. It was superseded by

Einstein's general theory of relativity

3. Gravity is a weak force.

- a. What is the force of gravity between two 1.0 kg masses 1.0 metres apart?

$$F_g = \frac{Gm_1m_2}{d^2} = \frac{6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg}\cdot\text{s}^2} \times 1.0 \text{ kg} \times 1.0 \text{ kg}}{(1.0 \text{ m})^2} = 6.67 \times 10^{-11} \frac{\text{kg}\cdot\text{m}}{\text{s}^2} = \cancel{6.67} = 6.67 \times 10^{-11} \text{ N [towards each other]}$$

- b. The masses are moved so that they are 1.0 mm apart. What is the force of gravity between the masses?

$$F_g = \frac{Gm_1m_2}{d^2} = \frac{6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg}\cdot\text{s}^2} \times 1.0 \text{ kg} \times 1.0 \text{ kg}}{(0.001 \text{ m})^2} = 6.67 \times 10^{-5} \text{ N [towards each other]}$$

- c. The masses are moved so that they are at opposite "ends" of the universe, 93 billion light years apart. What is the force of gravity between the masses?

$$d = 93 \times 10^9 \text{ light-years} \times \frac{9.461 \times 10^{15} \text{ m}}{\text{light year}} = 8.80 \times 10^{26} \text{ m}$$

$$F_g = \frac{Gm_1m_2}{d^2} = \frac{6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg}\cdot\text{s}^2} \times 1.0 \text{ kg} \times 1.0 \text{ kg}}{(8.80 \times 10^{26} \text{ m})^2} = 0.086 \times 10^{-63} \text{ N} = 8.6 \times 10^{-65} \text{ N [towards each other]}$$

4. Using the Universal Law of Gravitation, find the force of gravity on a 1 kg mass at the Earth's surface.

$$F_g = \frac{G m_1 m_2}{d^2} = \frac{6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2} \times 1.0 \text{ kg} \times 5.972 \times 10^{24} \text{ kg}}{(6371000 \text{ m})^2} = 9.8 \text{ N [down]}$$

- a. What will be the force of gravity on the 1 kg mass at the moon's surface? How does this compare to Earth's gravity?

$$F_g = \frac{G m_1 m_2}{d^2} = \frac{6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2} \times 1.0 \text{ kg} \times 7.35 \times 10^{22} \text{ kg}}{(1737000 \text{ m})^2} = 1.6 \text{ N [down]}$$

$$\frac{F_{g \text{ moon}}}{F_{g \text{ earth}}} = \frac{1.6 \text{ N}}{9.8 \text{ N}} \approx 16\% \approx \frac{1}{6}$$

- b. Using the Universal Law of Gravitation, find the force of gravity on a 1 kg mass on the International Space Station, which is located 400 km above the Earth's surface. How does this compare with the force of gravity at the surface?

$$F_g = \frac{G m_1 m_2}{d^2} = \frac{6.67 \times 10^{-11} \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2} \times 1.0 \text{ kg} \times 5.972 \times 10^{24} \text{ kg}}{(6371000 \text{ m} + 400000 \text{ m})^2} = 8.7 \text{ N [down]}$$

$$\frac{F_{g \text{ ISS}}}{F_{g \text{ earth}}} = \frac{8.7 \text{ N}}{9.8 \text{ N}} \approx 89\%$$

- c. If there is still gravity at the ISS, why do astronauts float?